# Course Description

The aim of this course is to cover modern tools for data-driven decision making. Most decision making tasks involve uncertainty that is directly impacted by the amount and complexity of data at hand. Classical decision models rely on strong distributional assumptions about the uncertain events. But in recent years, and due to growing availability of rich data, there has been a rapid adoption of models from machine learning and statistics that provide more accurate and personalized picture of the uncertainty which in turn leads to better decisions. The interplay between the multiple objectives of modeling the data, personalization, and decision optimization has created a number mathematical models that the course aims to cover.

### Topics<sup>1</sup>

- 1. The "Data  $\rightarrow$  prediction  $\rightarrow$  decision" paradigm. Methods: Parametric estimation and regularization Reference: Bayati et al. [\[7\]](#page-2-0).
- 2. Indirect and direct methods for learning and decision making in presence of covariates Methods: Non-parametric estimation, random forest References: Ban and Rudin [\[3\]](#page-1-0), Bertsimas and Kallus [\[8\]](#page-2-1).
- 3. Indirect and direct methods for learning and decision making for multi-outcome settings Methods: Matrix estimation, low-rank methods References: Kao and Van Roy [\[14\]](#page-2-2).
- 4. Multi-armed bandit, a toy model for dynamic learning and decision making Methods:  $\epsilon$ -Greedy, Upper Confidence Bound (UCB), Thompson Sampling References: Scott [\[17\]](#page-2-3), Chapelle and Li [\[10\]](#page-2-4).
- 5. Multi-armed bandits with covariates I Methods: Linear bandits, UCB and Thompson sampling for linear bandits References: Li et al. [\[15\]](#page-2-5), Abbasi-Yadkori et al. [\[1\]](#page-1-1), Agrawal and Goyal [\[2\]](#page-1-2), Russo and Van Roy [\[16\]](#page-2-6), Hamidi and Bayati [\[13\]](#page-2-7).
- 6. Multi-armed bandits with covariates II Methods: Two estimator bandits, lasso bandit for high-dimensional problems References: Goldenshluger and Zeevi [\[11\]](#page-2-8), Bastani and Bayati [\[4\]](#page-1-3).
- 7. Free exploration in contextual bandits Methods: Matrix tail bounds, covariate diversity, Greedy-First algorithm References: Bastani et al. [\[5\]](#page-1-4), Bietti et al. [\[9\]](#page-2-9).
- 8. Bayesian learning and decision-making Methods: Factor graphs and message-passing algorithms References: Graepel and Herbrich [\[12\]](#page-2-10), Bayati and Montanari [\[6\]](#page-2-11).

<sup>&</sup>lt;sup>1</sup>There may be some modifications to this list as the quarter unfolds

## Logistics

Time and Location. Thursdays 3 PM - 5:50 PM over zoom (links will be provided on Canvas).

Prerequisites. Knowledge of probability and linear algebra is required. Some assignments may need programming in one language of your preference (e.g. Matlab, Python,  $R, \ldots$ )

Course Calendar. Contains the schedule and due dates, [this link.](https://docs.google.com/spreadsheets/d/1kJrCEkP448XLx-vsvXcYF_7BaCglt3LCnL_mIM1bB7s/edit#gid=0)

#### Grading Criteria and Policies

- 1. Class participation (20%)
	- Scribing lecture notes, we provide you with a LaTeX template (make your selections on [\(course calendar,](https://docs.google.com/spreadsheets/d/1kJrCEkP448XLx-vsvXcYF_7BaCglt3LCnL_mIM1bB7s/edit#gid=0) contains the schedule and due dates))
- 2. Two Problem set (20%)
- 3. Projects (50%), you can work with teams of size up to three (we strongly encourage at least two)
	- Proposal, one page  $(5\%)$
	- Progress report, two pages  $(10\%)$
	- Final presentation (15-20 minutes, depending on the number of projects), during last lecture (15%)
	- Final report (at most 5 pages)  $(10\%)$

#### References

- <span id="page-1-1"></span>[1] Yasin Abbasi-Yadkori, Dávid Pál, and Csaba Szepesvári. Improved algorithms for linear stochastic bandits. In NIPS, pages 2312–2320, 2011.
- <span id="page-1-2"></span>[2] Shipra Agrawal and Navin Goyal. Thompson sampling for contextual bandits with linear payoffs. In *ICML*, pages 127–135, 2013.
- <span id="page-1-0"></span>[3] Gah-Yi Ban and Cynthia Rudin. The big data newsvendor: Practical insights from machine learning. Operations Research, 67(1):90–108, 2019. doi: 10.1287/opre.2018. 1757. URL <https://doi.org/10.1287/opre.2018.1757>.
- <span id="page-1-3"></span>[4] H. Bastani and M. Bayati. Online decision-making with high-dimensional covariates. [https://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=2661896](https://papers.ssrn.com/sol3/papers.cfm?abstract_id=2661896), 2015.
- <span id="page-1-4"></span>[5] H. Bastani, M. Bayati, and K. Khosravi. Mostly exploration-free algorithms for contextual bandits. <https://arxiv.org/abs/1704.09011>.
- <span id="page-2-11"></span>[6] M. Bayati and A. Montanari. The dynamics of message passing on dense graphs, with applications to compressed sensing. IEEE Transactions on Information Theory, 57: 764–785, 2011.
- <span id="page-2-0"></span>[7] M. Bayati, M. Braverman, M. Gillam, K. Mack, G. Ruiz, M. Smith, and E. Horvitz. Data-driven decisions for reducing readmissions for heart failure: General methodology and case study. PLOS ONE, 9, 2014. doi: 10.1371/journal.pone.0109264.
- <span id="page-2-1"></span>[8] Dimitris Bertsimas and Nathan Kallus. From predictive to prescriptive analytics. <https://arxiv.org/abs/1402.5481>, 2014.
- <span id="page-2-9"></span>[9] Alberto Bietti, Alekh Agarwal, and John Langford. A Contextual Bandit Bake-off. arXiv e-prints, art. arXiv:1802.04064, Feb 2018.
- <span id="page-2-4"></span>[10] Olivier Chapelle and Lihong Li. An empirical evaluation of thompson sampling. In J. Shawe-Taylor, R. S. Zemel, P. L. Bartlett, F. Pereira, and K. Q. Weinberger, editors, Advances in Neural Information Processing Systems 24, pages 2249–2257. Curran Associates, Inc., 2011. URL [http://papers.nips.cc/paper/](http://papers.nips.cc/paper/4321-an-empirical-evaluation-of-thompson-sampling.pdf) [4321-an-empirical-evaluation-of-thompson-sampling.pdf](http://papers.nips.cc/paper/4321-an-empirical-evaluation-of-thompson-sampling.pdf).
- <span id="page-2-8"></span>[11] Alexander Goldenshluger and Assaf Zeevi. A linear response bandit problem. Stochastic Systems, 3(1):230–261, 2013.
- <span id="page-2-10"></span>[12] Thore Graepel and Ralf Herbrich. Large Scale Data Analysis and Modelling in Online Services and Advertising. In Proceedings of the 14th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining, page 2, Las Vegas, 2008. URL <http://www.herbrich.me/papers/kdd2008.pdf>.
- <span id="page-2-7"></span>[13] Nima Hamidi and Mohsen Bayati. A General Theory of the Stochastic Linear Bandit and Its Applications. 2020. doi: 10.48550/ARXIV.2002.05152. URL [https://arxiv.](https://arxiv.org/abs/2002.05152) [org/abs/2002.05152](https://arxiv.org/abs/2002.05152).
- <span id="page-2-2"></span>[14] Yi-Hao Kao and Benjamin Van Roy. Directed principal component analysis. Operations Research, 62(4):957–972, 2014. doi: 10.1287/opre.2014.1290.
- <span id="page-2-5"></span>[15] Lihong Li, Wei Chu, John Langford, and Robert E. Schapire. A contextual-bandit approach to personalized news article recommendation. In Proceedings of the 19th International Conference on World Wide Web, WWW '10, pages 661–670, New York, NY, USA, 2010. ACM. ISBN 978-1-60558-799-8. doi: 10.1145/1772690.1772758. URL <http://doi.acm.org/10.1145/1772690.1772758>.
- <span id="page-2-6"></span>[16] Daniel Russo and Benjamin Van Roy. Learning to optimize via posterior sampling. Mathematics of Operations Research, 39(4):1221–1243, 2014.
- <span id="page-2-3"></span>[17] Steven L. Scott. A modern bayesian look at the multi-armed bandit. Appl. Stoch. Model. Bus. Ind., 26(6):639–658, November 2010. ISSN 1524-1904. doi: 10.1002/asmb.874. URL <http://dx.doi.org/10.1002/asmb.874>.